

Name: _____

Date: _____

Circles: Arc Lengths and Areas of a Sector

An **arc** is an unbroken part of a circle consisting of all points on a circle located between two endpoints. There are three classifications of arcs: the *minor arc*, the *major arc*, and the *semicircle*. **Arc length** is the distance along an arc measured in linear units. It is calculated by multiplying the circumference ($2\pi r$) by the angle of the arc divided by the total number of possible angles in a circle.

$$L = 2\pi r \left(\frac{m^\circ}{360^\circ} \right) \quad \text{Circumference} \left(\frac{\text{Angle measure of the arc}}{\text{Total degrees in a circle}} \right)$$

A **sector** is a region bound by two radii of the circle and their intercepted arc. We can use the following formula to find the **area of a sector**:

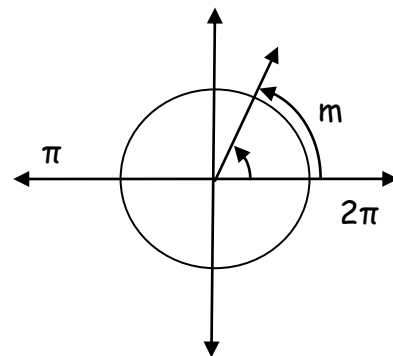
$$A = \pi r^2 \left(\frac{m^\circ}{360^\circ} \right) \quad \text{Area of circle} \left(\frac{\text{Angle measure of the arc}}{\text{Total degrees in a circle}} \right)$$

Did you notice the similarities between the two formulas? Both use the proportion of angle measures in order to derive the desired information. A similar system was established using **radians**.

Radians determine a sector's area in proportion to the rest of a circle. In a circle with radius r and center at the origin, one radian is the measure of an angle in standard position whose terminal side intercepts an arc with length m .

Radians are angle measurements separate from degrees, so that 360° converts to 2π radians and 180° converts to π radians.

We can use this proportion to convert radian angle measure to degrees and vice-versa.



Degrees to Radians: $\frac{\pi \text{ radians}}{180^\circ}$
Multiply degree measure by

Radians to Degrees: $\frac{180^\circ}{\pi \text{ radians}}$
Multiply radian measure by

Name: _____

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Practice. Calculate the arc length using the given information.

1. $r = 7$
 $m = 60$

2. $r = 29$
 $m = 18$

3. $r = 19$
 $m = 120$

4. $r = 28$
 $m = 180$

Practice. Calculate the area of the sector using the given information.

5. $r = 6$
 $m = 60$

6. $r = 10$
 $m = 30$

7. $r = 3$
 $m = 90$

8. $r = 15$
 $m = 12$

Practice. Convert from radians to degrees, or degrees to radians.

9. $\frac{2\pi}{3}$

10. 60°

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Answer Key

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1. 7.33

2. 9.11

3. 39.77

4. 87.92

5. 18.84

6. 26.17

7. 7.07

8. 23.55

9. 120°

10. $\frac{\pi}{3}$